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Speculation ("Théorie de la spéculation", published 1900) with the introduction of the most basic and most influential of processes, Brownian motion, and its applications to the pricing of options.[4][5] Brownian motion is derived using the Langevin equation and the discrete random walk.[6] Bachelier modeled the time series of changes in the logarithm of stock prices as a random walk in which the short-term changes had a finite variance. This causes longer-term changes to follow a Gaussian distribution.[7] The theory remained dormant until Fischer Black and Myron Scholes, along with fundamental contributions by Robert C. Merton, applied the second most influential process, the geometric Brownian motion, to option pricing. For this M. Scholes and R. Merton were awarded the 1997 Nobel Memorial Prize in Economic Sciences. Black was ineligible for the prize because he died in 1995.[8] The next important step was the fundamental theorem of asset pricing by Harrison and Pliska (1981), according to which the suitably normalized current price P0 of security is arbitrage-free, and thus truly fair only if there exists a stochastic process Pt with constant expected value which describes its future evolution:[9] 




P

0


=
E
0


(

P

t


)


{\displaystyle P\_{0}=\mathbf {E} \_{0}(P\_{t})}

 1 A process satisfying (1) is called a "martingale". A martingale does not reward risk. Thus the probability of the normalized security price process is called "risk-neutral" and is typically denoted by the blackboard font letter "



Q


{\displaystyle \mathbb {Q} }

". The relationship (1) must hold for all times t: therefore the processes used for derivatives pricing are naturally set in continuous time. The quants who operate in the Q world of derivatives pricing are specialists with deep knowledge of the specific products they model. Securities are priced individually, and thus the problems in the Q world are low-dimensional in nature. Calibration is one of the main challenges of the Q world: once a continuous-time parametric process has been calibrated to a set of traded securities through a relationship such as (1), a similar relationship is used to define the price of new derivatives. The main quantitative tools necessary to handle continuous-time Q-processes are Itô's stochastic calculus, simulation and partial differential equations (PDEs).[10] The P world Goal "model the future" Environment real-world probability 



P


{\displaystyle \mathbb {P} }

 Processes discrete-time series Dimension large Tools multivariate statistics Challenges estimation Business buy-side Risk and portfolio management aims to model the statistically derived probability distribution of the market prices of all the securities at a given future investment horizon. This "real" probability distribution of the market prices is typically denoted by the blackboard font letter "



P


{\displaystyle \mathbb {P} }

", as opposed to the "risk-neutral" probability "



Q


{\displaystyle \mathbb {Q} }

" used in derivatives pricing. Based on the P distribution, the buy-side community takes decisions on which securities to purchase in order to improve the prospective profit-and-loss profile of their positions considered as a portfolio. Increasingly, elements of this process are automated; see Outline of finance § Quantitative investing for a listing of relevant articles. For their pioneering work, Markowitz and Sharpe, along with Merton Miller, shared the 1990 Nobel Memorial Prize in Economic Sciences, for the first time ever awarded for a work in finance. The portfolio-selection work of Markowitz and Sharpe introduced mathematics to investment management. With time, the mathematics has become more sophisticated. Thanks to Robert Merton and Paul Samuelson, one-period models were replaced by continuous time, Brownian-motion models, and the quadratic utility function implicit in mean–variance optimization was replaced by more general increasing, concave utility functions.[11] Furthermore, in recent years the focus shifted toward estimation risk, i.e., the dangers of incorrectly assuming that advanced time series analysis alone can provide completely accurate estimates of the market parameters. [12] See Financial risk management § Investment management. Much effort has gone into the study of financial markets and how prices vary with time. Charles Dow, one of the founders of Dow Jones & Company and The Wall Street Journal, enunciated a set of ideas on the subject which are now called Dow Theory. This is the basis of the so-called technical analysis method of attempting to predict future changes. One of the tenets of "technical analysis" is that market trends give an indication of the future, at least in the short term. The claims of the technical analysts are disputed by many academics.[citation needed] While numerous empirical studies have examined the effectiveness of technical analysis, there remains no definitive consensus on its usefulness in forecasting financial markets.[13] Further information: Financial economics § Challenges and criticism, and Financial engineering § Criticisms See also: Financial models with long-tailed distributions and volatility clustering Over the years, increasingly sophisticated mathematical models and derivative pricing strategies have been developed, but their credibility was damaged by the 2008 financial crisis. Contemporary practice of mathematical finance has been subjected to criticism from figures within the field notably by Paul Wilmott, and by Nassim Nicholas Taleb, in his book The Black Swan.[14] Taleb claims that the prices of financial assets cannot be characterized by the simple models currently in use, rendering much of current practice at best irrelevant, and, at worst, dangerously misleading. Wilmott and Emanuel Derman published the Financial Modelers' Manifesto in January 2009[15] which addresses some of the most serious concerns. Bodies such as the Institute for New Economic Thinking are now attempting to develop new theories and methods.[16] In general, modeling the changes by distributions with finite variance is, increasingly, said to be inappropriate.[17] In the 1960s it was discovered by Benoit Mandelbrot that changes in prices do not follow a Gaussian distribution, but are rather modeled better by Lévy alpha-stable distributions.[18] The scale of change, or volatility, depends on the length of the time interval to a power a bit more than 1/2. Large changes up or down are more likely than what one would calculate using a Gaussian distribution with an estimated standard deviation. But the problem is that it does not solve the problem as it makes parametrization much harder and risk control less reliable.[14] Perhaps more fundamental: though mathematical finance models may generate a profit in the short-run, this type of modeling is often in conflict with a central tenet of modern macroeconomics, the Lucas critique - or rational expectations - which states that observed relationships may not be structural in nature and thus may not be possible to exploit for public policy or for profit unless we have identified relationships using causal analysis and econometrics.[19] Mathematical finance models do not, therefore, incorporate complex elements of human psychology that are critical to modeling modern macroeconomic movements such as the self-fulfilling panic that motivates bank runs. See also: Outline of finance § Financial mathematics, Outline of finance § Mathematical tools, Outline of finance § Derivatives pricing, Outline of corporate finance, and Computational finance Asymptotic analysis Backward stochastic differential equation Calculus Copulas, including Gaussian Differential equations Expected value Ergodic theory Feynman–Kac formula Finance § Quantitative finance Fourier transform Girsanov theorem Itô's lemma Martingale representation theorem Mathematical models Mathematical optimization Linear programming Nonlinear programming Quadratic programming Monte Carlo method Numerical analysis Gaussian quadrature Real analysis Partial differential equations Heat equation Numerical partial differential equations Crank–Nicolson method Finite difference method Probability Probability distributions Binomial distribution Johnson's SU-distribution Log-normal distribution Student's t-distribution Quantile functions Radon–Nikodym derivative Risk-neutral measure Scenario optimization Stochastic calculus Brownian motion Lévy process Stochastic differential equation Stochastic volatility Survival analysis Value at risk Volatility ARCH model GARCH model The Brownian model of financial markets Rational pricing assumptions Risk neutral valuation Arbitrage-free pricing Valuation adjustments Credit valuation adjustment XVA Yield curve modelling Multi-curve framework Bootstrapping Construction from market data Fixed-income attribution Nelson–Siegel Principal component analysis Forward Price Formula Futures contract pricing Swap valuation Currency swap#Valuation and Pricing Interest rate swap#Valuation and pricing Multi-curve framework Variance swap#Pricing and valuation Asset swap #Computing the asset swap spread Credit default swap #Pricing and valuation Options Put–call parity (Arbitrage relationships for options) Intrinsic value, Time value Moneyness Pricing models Black–Scholes model Black model Binomial options model Implied binomial tree Edgeworth binomial tree Monte Carlo option model Implied volatility, Volatility smile Local volatility Stochastic volatility Constant elasticity of variance model Heston model Stochastic volatility jump SABR volatility model Markov switching multifractal The Greeks Finite difference methods for option pricing Vanna–Volga pricing Trinomial tree Implied trinomial tree Garman–Kohlhagen model Lattice model (finance) Margrabe's formula Carr–Madan formula Pricing of American options Barone-Adesi and Whaley Bjerk sund and Stensland Black's approximation Least Square Monte Carlo Optimal stopping Roll-Geske–Whaley Interest rate derivatives Black model caps and floors swaptions Bond options Short-rate models Rendleman–Bartter model Vasicek model Ho–Lee model Hull–White model Cox–Ingersoll–Ross model Black–Karasinski model Black–Derman–Toy model Kalotay–Williams–Fabozzi model Longstaff–Schwartz model Chen model Forward rate-based models LIBOR market model Financial engineering Financial modeling § Quantitative finance International Association for Quantitative Finance International Swaps and Derivatives Association List of economists Master of Quantitative Finance Outline of finance Physics of financial markets Quantitative behavioral finance Quantum finance Rocket science (finance) Statistical finance Technical analysis XVA ^ "Quantitative Finance". 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